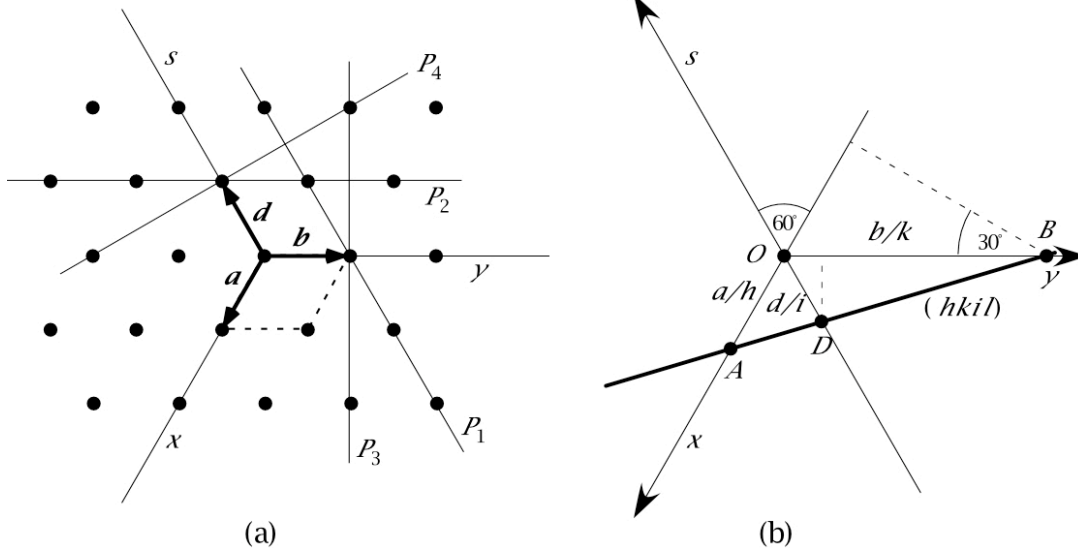


Problem 1 (20 points)



(a) Figure (a) shows a hexagonal lattice in [001] projection. Argue why the planes P_1 and P_2 (all planes parallel to the z -axis) are symmetrically equivalent to each other. This is also true for P_3 and P_4 . Determine the Miller indices (hkl) of $P_1, P_2, P_3,$ and P_4 .

(b) Although P_1 and P_2 symmetrically equivalent to each other, their Miller indices (hkl) are different. This is the same for the planes P_3 and P_4 . For this reason, one introduces a fourth axes, s , and a fourth fundamental translation, d . In this system, lattice planes are described by “Miller-Bravais” indices $(hkil)$, where h reflects in how many equal parts the planes divide a , k reflects in how many equal parts the planes divide b , i reflects in how many equal parts the planes divide d , and l reflects in how many equal parts the planes divide c .

Determine the Miller-Bravais indices $(hkil)$ of P_1, P_2, P_3 and P_4 . Note that the Miller-Bravais indices reflect that P_1 and P_2 are of the same type and P_3 and P_4 are of the same type.

(c) Considering Fig. (b), show that for any set $(hkil)$ of planes the sum of the first three Miller-Bravais indices vanishes: $h + k + i = 0$

Hint: Equate the area of the triangle OAB to the sum of the areas of OAD and ODB , and express the areas of these triangles with the Miller-Bravais indices.

(d) Lattice directions are expressed by Weber indices $[uvtw]$ in the four-axis system.

Without an additional condition, however, the notation would be ambiguous (e.g. the x

direction could be written as $[1000]$ or $[0\bar{1}\bar{1}0]$). Therefore, one requires $u + v + t = 0$.

Respecting this condition, (i) express the Weber indices u, v, t, w as a function of the conventional (Miller) indices U, V, W (use capital letters for distinction), and (ii) express the conventional indices U, V, W as a function of the Weber indices u, v, t, w .

(e) Show that the normal to the plane $(hkil)$ will have indices $[defg] = h, k, i, \frac{3a^2}{2c^2}l$.

Problem 2 (10 points)

Prove that for a crystal with proper rotation C_n , n can only be 1, 2, 3, 4 or 6.

Hint: Consider the definition of rotation symmetry. If you start with a row of lattice points, rotate by an angle of $2\pi/n$, you can get another row of lattice points, which must be compatible with the translation symmetry of the crystal.

Problem 3 (10 points)

(a) According to the resistivity versus temperature graph shown in the following figure, determine the temperature coefficient of resistivity of pure iron and of electrotechnical steel (Fe with 4% C), which are used in various electrical machinery, at two temperatures: 0 °C and 500 °C.

(b) Argue the differences of the resistivity of the two materials and the differences of temperature coefficients of resistivity.

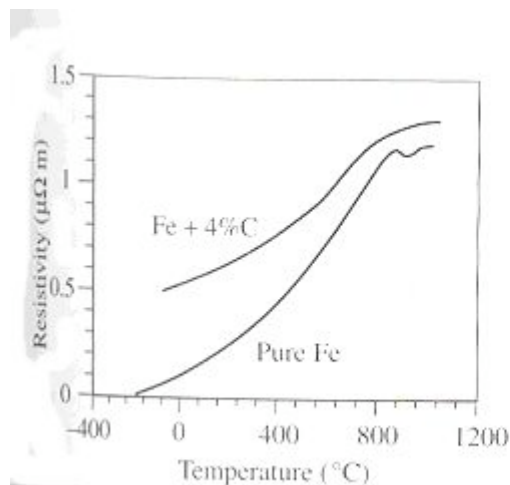


Figure 2.33 Resistivity versus temperature for pure iron and 4% C steel.

Problem 4 (10 points)

(a) As shown in the textbook, the Hall coefficient for electron conduction is given

by $R_H = \frac{1}{en}$. Prove that the Hall coefficient for materials with only positive charge

carriers (e.g. holes in a semiconductor) is $R_H = \frac{1}{ep}$, where p is the carrier concentration.

(b) In the case of an intrinsic semiconductor, such as pure GaAs, the electron and hole concentrations and drift mobilities at 300 K are given as $n = p = 1.8 \times 10^6 \text{ cm}^{-3}$,

$\mu_e = 8500 \text{ cm}^2 / \text{Vs}$ and $\mu_h = 400 \text{ cm}^2 / \text{Vs}$. Calculate the Hall coefficient and compare it with that of copper (refer to Table 2.4 in the textbook).