

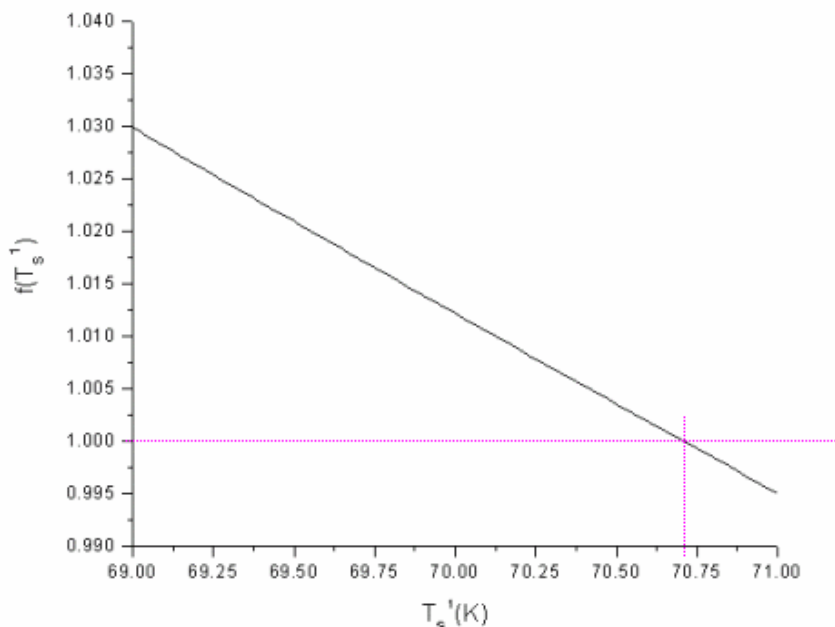
**Problem 2— “temperature dependence of conductivity”**

$$c) N_c' = 2 \left( \frac{2\pi m_e^* k}{h^2} T \right)^{3/2} = 2.8 \times 10^{19} \times \left( \frac{T_s'}{300} \right)^{1.5} = (T_s')^{1.5} \times 5.389 \times 10^{15} \text{ cm}^{-3}$$

$$T_s' = \frac{\Delta E}{k \ln \frac{N_c'}{2N_d}} = \frac{0.045 \times 1.6 \times 10^{-19}}{1.38 \times 10^{-23} \times \ln \frac{(T_s')^{1.5} \times 5.389 \times 10^{15}}{2 \times 10^{15}}}$$

$$\text{Consider function } f(T_s') = \frac{1}{T_s'} \times \frac{0.045 \times 1.6 \times 10^{-19}}{1.38 \times 10^{-23} \times \ln \frac{(T_s')^{1.5} \times 5.389 \times 10^{15}}{2 \times 10^{15}}} = \frac{1}{T_s'} \times \frac{521.74}{[0.9912 + 1.5 \ln T_s']}$$

We can plot  $f(T_s')$  vs  $T_s'$  curve, as shown in the following diagram. The exact value of  $T_s'$  is given by  $f(T_s') = 1$ , i.e.  $T_s' = 70.70\text{K}$ . **The above solution will give +3 bonus points.**



**Problem 4—“thermal drift in semiconductor devices”**

a) The potential of the cold side with respect to the hot side is taken as the sign of the Seebeck voltage and hence the Seebeck coefficient  $S$ . Thus, if electrons diffuse from hot to cold, then the Seebeck voltage (and hence  $S$ ) is negative, and if holes diffuse from hot to cold then the Seebeck voltage is positive. The equation given in (b) only gives the magnitude of  $S$ .

This provides a convenient way to identify whether a semiconductor is doped  $n$ -type or  $p$ -type. If the hot side is positive with respect to the cold side then the semiconductor is  $n$ -type. If the hot side is negative then it is  $p$ -type. The simplest test is to touch the test leads of a voltmeter (1-10 mV range) to a semiconductor with one lead made hot. In reality, the semiconductor and the copper lead form a thermocouple but the Seebeck coefficient of the semiconductor is much greater than that of the metal lead.